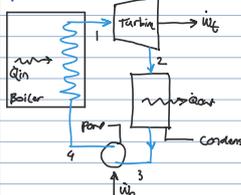


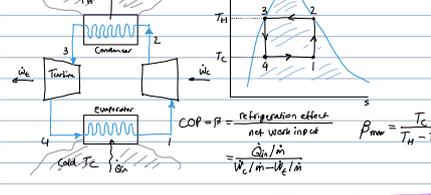
# Ran kinu cycle



**1 Turbine**  
 $W_t = \dot{Q}_{in} - \dot{m}(h_1 - h_2)$   
**2 Pump (Internally reversible)**  
 $W_p = \dot{Q}_{out} - \dot{m}(h_3 - h_4)$   
 $\dot{W}_m = -\int T ds + h_3 - h_4$   
 $= \int_3^4 v dp = v_3 (P_4 - P_3) = h_4 - h_3$   
 $P_4 = P_1$   
 $P_3 = P_2$   
 $x = \frac{h_4 - h_3}{h_2 - h_1}$

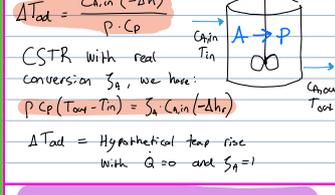
**Losses in Turbine & Pump**  
**Superheat**  
 $\eta_t = \frac{h_1 - h_2}{h_1 - h_{2s}}$   
 $\eta_p = \frac{h_4 - h_3}{h_{4s} - h_3}$   
 $\eta_p = \frac{v_3 (P_4 - P_3)}{v_3 (P_4 - P_3) + \dot{Q}_{loss}}$

# Carnot Refrigeration Cycle



$COP = \beta = \frac{\text{ref. effect}}{\text{net work input}} = \frac{Q_{in}/\dot{m}}{W_{net}/\dot{m}}$   
 $P_{max} = \frac{T_c}{T_H - T_c}$   
 $\eta_c = \frac{W_t/\dot{m}}{W_c/\dot{m}} = \frac{h_1 - h_2}{h_1 - h_3}$

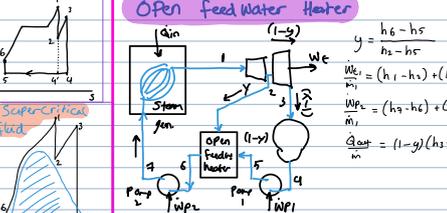
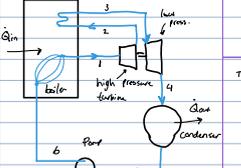
# Adiabatic Temperature Rise CSTR



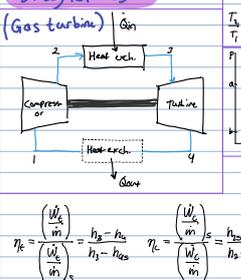
$\Delta T_{ad} = \frac{C_{in}(-\Delta h)}{P \cdot C_p}$   
 CSTR with real conversion  $X_A$ , we have:  
 $P C_p (T_{out} - T_{in}) = S_A (-\Delta h)$   
 $\Delta T_{ad} = \text{Hypothetical temp rise with } Q=0 \text{ and } S_A=1$

**Exergic rate balance open system**  
 $0 = \sum_j (1 - \frac{T_0}{T_j}) \dot{Q}_j - \dot{W} + \sum \dot{m}_i e_i - \sum \dot{m}_e e_e - \dot{E}_d$   
 $e_f = h - h_0 - T_0(s - s_0) + \frac{v^2}{2} + z$  (specific flow exergy)  
 $e_c = (1 - \frac{T_0}{T_c}) T_0 (s - s_0) + h - h_0 + \frac{v^2}{2} + z$  (exergy loss)

# Reheat

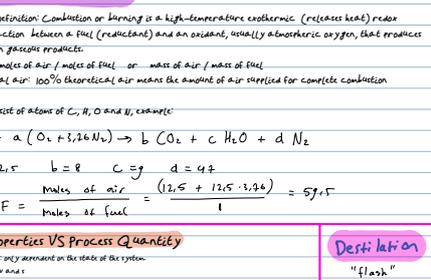


# Brayton Cycle



**Adiabatic compression/expansion ideal gas**  
 $\frac{T_2}{T_1} = (\frac{P_2}{P_1})^{\frac{\gamma-1}{\gamma}}$   
 $K = \frac{C_p}{C_v} = \frac{\gamma}{\gamma-1}$   
**Thermal efficiency**  
 $\eta = \frac{C_p(T_3 - T_4) - C_p(T_1 - T_2)}{C_p(T_3 - T_2)}$   
 $= 1 - \frac{T_4 - T_1}{T_3 - T_2}$   
 $= 1 - (\frac{P_2}{P_1})^{\frac{\gamma-1}{\gamma}}$

# Vapor Compression Refr. Syst.



$COP = \beta = \frac{\text{ref. effect}}{\text{net work}} = \frac{Q_{in}/\dot{m}}{W_{net}/\dot{m}}$   
 $\eta_c = \frac{W_t/\dot{m}}{W_c/\dot{m}} = \frac{h_1 - h_2}{h_1 - h_3}$

# Exergic (second law) efficiency

**Balance:**  
 $(1 - \frac{T_0}{T_c}) \dot{Q}_s = (1 - \frac{T_0}{T_u}) \dot{Q}_u + \dot{E}_d$   
**First law efficiency:**  $\eta = \frac{\dot{Q}_u}{\dot{Q}_s}$   
**Second law efficiency:**  $\epsilon = \frac{(1 - \frac{T_0}{T_u}) \dot{Q}_u}{(1 - \frac{T_0}{T_s}) \dot{Q}_s}$   
 $\epsilon = \eta \frac{(1 - T_0/T_u)}{(1 - T_0/T_s)}$

# Reactors

$S_A = \frac{n_{Ao} - n_A}{n_{Ao}} = \frac{C_{Ao} - C_A}{C_{Ao}} = 1 - \frac{C_A}{C_{Ao}}$   
 $\sigma_A = \frac{C_0}{C_{Ao} - C_A}$   
 $\eta_A = \sum_i S_A \sigma_A = \frac{C_0}{C_{Ao} - C_A} \frac{C_{Ao} - C_A}{C_{Ao}} = \frac{C_0}{C_{Ao}}$

**Batch reactor**  
 $A \rightarrow P \quad r_A = -k_1 C_A$   
 $\frac{dC_A}{dt} = -k_1 C_A \Rightarrow C_A(t) = C_{Ao} e^{-k_1 t}$   
 max yield:  $t = \frac{1}{k_1} \ln(\frac{C_{Ao}}{C_A})$   
 $\frac{d\eta}{dt} = 0$

# Fluidized bed reactor

$U_{MF} = \frac{d_p^2 (\rho_s - \rho_f) g}{150 \mu (1 - \epsilon)^2} \rightarrow Re_p < 5$  (low air)  
 $U_{MF} = \frac{d_p^2 (\rho_s - \rho_f) g}{180 \mu} \rightarrow Re_p > 500$  (high air)  
 → if  $5 < Re_p < 500$  both terms!

$\frac{dP}{dz} = (\rho_s - \rho_f)(1 - \epsilon) g$   
 $\frac{dP}{dz} = \frac{150 \mu (1 - \epsilon)^2}{d_p^2} U_{MF} + \frac{180 \mu (\rho_s - \rho_f) (1 - \epsilon)^2}{d_p^2} U_{MF}$   
 $\rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

# Packed bed reactor

pressure drop across a bed of particles:  
 $\Delta P = \frac{150 \mu L (1 - \epsilon)^2}{d_p^2} v_0 + \frac{1.75 L \rho (1 - \epsilon) v_0^2}{d_p}$   
 $A = \text{viscosity [Pa.s]}$   
 $\rho = \text{fluid density}$   
 $L = \text{bed length}$   
 $d_p = \text{particle D}$   
 $v_0 = E(v) \cdot \text{superficial velocity}$   
 $\langle v \rangle = \text{avg axial velocity}$   
 $E = \text{bed porosity}$   
 $1 - \epsilon = \text{solid volume fraction}$   
 $v_0 = E(v) \cdot \text{superficial velocity}$   
 $\langle v \rangle = \text{avg axial velocity}$

# Combustion

**Combustion Definition:** Combustion or burning is a high-temperature exothermic (releases heat) redox chemical reaction between a fuel (reductant) and an oxidant, usually atmospheric oxygen, that produces oxidized, often gaseous products.  
 - AF Ratio: moles of air / moles of fuel or mass of air / mass of fuel  
 - Theoretical air: 100% theoretical air means the amount of air sufficient for complete combustion  
 Reaction consist of atoms of C, H, O and N, example:  
 $C_8 H_{18} + a(O_2 + 3.76 N_2) \rightarrow b CO_2 + c H_2O + d N_2$   
 $a = 12.5 \quad b = 8 \quad c = 9 \quad d = 47$   
 Moles of air =  $(12.5 + 12.5 \cdot 3.76) = 57.8$   
 AF =  $\frac{\text{Moles of fuel}}{\text{Moles of air}} = \frac{1}{57.8}$

# Stoichiometric Properties VS Process Quantity

Stoichiometric properties only dependent on the state of the system.  
 For example:  $T, P, v, \dots$   
 Process Quantity: Dependent on the way a process is executed.

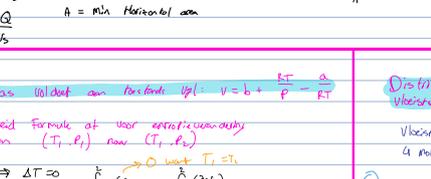
# Extensive state properties VS non extensive state properties

Extensive: making the system 'n' larger, makes the property 'n' larger.  
 For example:  $V, S, H, C_p, C_v$   
 Intensive: not dependent on amount of material.  
 For example:  $T, P, \rho, \epsilon, \mu, \dots$

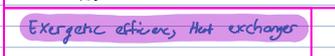
# Equation of state

Relation between pressure, temperature, density, composition  
**Iso-lines**  
 - isobar: constant pressure  
 - isochor: constant volume  
 - isochor: constant molar volume (v)  
 - isochor: constant entropy process (s)

# Sedimentation



# Destillation



# Exergic efficiency Heat exchanger

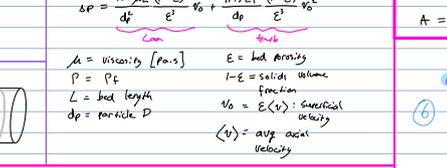
**Balance:**  
 $0 = \dot{m}_h c_p (T_h - T_{h0}) + \dot{m}_c c_p (T_c - T_{c0}) - \dot{m}_h c_p T_c - \dot{m}_c c_p T_h - \dot{E}_d$   
**Efficiency:**  
 $\epsilon = \frac{\dot{m}_c (e_{c2} - e_{c1})}{\dot{m}_h (e_{h1} - e_{c1})}$

# CSTR

Residence time:  $\tau = \frac{V_0}{\dot{V}}$   
 max operating  $d\tau \rightarrow 0$

**Plug flow**  
 $\frac{dC_A}{dt} = -r_A \frac{L}{v}$

# Activation energy



# Gas velocity in packed bed: $v = v_0 + \frac{v_f}{\epsilon} = \frac{Q}{A \epsilon}$

6) **Leit Formule at van der Waals equation**  
 Van  $(T, P)$  naar  $(T, v_0)$   
 $\Rightarrow \Delta T = 0$   
 $S_2 - S_1 = \int_1^2 \frac{C_p}{T} dT - \int_1^2 \left( \frac{\partial v}{\partial T} \right)_P dT$   
 $\left( \frac{\partial v}{\partial T} \right)_P = \frac{R}{P} + \frac{a}{T^2 P}$   
 $\Delta S_1 = - \int_1^2 \left( \frac{R}{P} + \frac{a}{T^2 P} \right) dT$   
 $= - \left[ R \ln \left( \frac{P_2}{P_1} \right) + \frac{a}{T^2} (P_2 - P_1) \right]$

# Distributie van een component in niet-neighbor

Wisselt A & B niet neighbor.  
 4 mol A, 3 mol B, 4 mol X → Na evenwicht:  $X_A^A = 0.2$

# Formule alle de abnauze de verhouding $\frac{T_1}{T_2}$ kan worden berekend

9)  $\ln \left( \frac{P_1}{P_2} \right) = \frac{a}{T_1^2} (P_1 - P_2) + \frac{R}{P_1} \ln \left( \frac{P_1}{P_2} \right)$

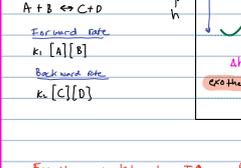
# Bereken K

$K = \frac{X_A^A}{X_B^B} = \frac{n_A^A}{n_B^B} = 4$   
 $X_A^A = 0.2 = \frac{n_A^A}{n_A^A + n_B^B} \Rightarrow 0.2(4 + 0.2 n_B^B) = n_A^A$   
 $n_B^B = 1$   
 $n_A^A = 3 \Rightarrow X_A^A = \frac{3}{3+3} = \frac{1}{2}$   
 $K = \frac{0.2}{0.2} = 0.14$

# 1 mol A toevoegd. Bereken $X_A^A$ na evenwicht

A = 1 mol: 5 mol A &  $n_A^A = X$   
 B = 1 mol: 3 mol B &  $n_B^B = 4 - X$   
 $X_A^A = \frac{X}{5+X} \quad X_B^B = \frac{4-X}{7-X}$   
 $K = 0.14 = \frac{X_A^A}{X_B^B}$   
 $0.14 = \frac{X(7-X)}{(5+X)(3-X)}$   
 $X = 1.1973$   
 $n_A^A = 1.1973 \quad X_A^A = \frac{1.1973}{5+1.1973} = 0.1973$

# Stoom turbine + condensator



$P_1 = 90 \text{ bar}$   
 $h_1 = 2901 \text{ kJ/kg}$   
 $\dot{Q}_{out} = h_3 - h_{c1}$   
 $\dot{Q}_{out} = 2162.8 \text{ kJ/kg}$   
 $h_3 = \frac{\dot{Q}_{out}}{\dot{m}} + h_{c1}$   
 $= 2162.8 + 173.88 = 2336.68$   
 $x_2 = \frac{h_2 - h_f}{h_g - h_f} = \frac{2336.68 - 171.98}{2577.0 - 173.88} = 0.90$

# Formule alle de abnauze de verhouding $\frac{T_1}{T_2}$ kan worden berekend

10)  $\ln \left( \frac{P_1}{P_2} \right) = \frac{a}{T_1^2} (P_1 - P_2) + \frac{R}{P_1} \ln \left( \frac{P_1}{P_2} \right)$

# Hoort de waarde v op van dit gas in de tank at?

8)  $\Rightarrow$  als dit is is:  $\left( \frac{dP}{dT} \right)_T \neq 0$   
 $-T \left( \frac{dP}{dT} \right)_T = 3 \frac{a}{T^2} \neq 0 \Rightarrow$  ja hoort in f at

# Ed

$\frac{\dot{E}_d}{\dot{m}} = -\frac{\dot{W}_t}{\dot{m}} + (e_{f1} - e_{f2})$   
 $\frac{\dot{W}_t}{\dot{m}} = h_1 - h_2 = 405 \text{ mJ/kg}$   
 $e_{f1} - e_{f2} = h_1 - h_2 - T_0(s_1 - s_2)$   
 $s_1 = 5.6172$   
 $s_2 = X_2(s_g - s_f) + s_f = 7.465$   
 $\frac{\dot{E}_d}{\dot{m}} = -405.142 + (2901.1 - 2336.68) - 300(5.6172 - 7.465) = -536.37 \text{ kJ/kg}$

# Formule alle de abnauze de verhouding $\frac{T_1}{T_2}$ kan worden berekend

11)  $\eta = \frac{(h_1 - h_2) - (h_{u1} - h_{u2})}{h_1 - h_{u1}}$   
 $\eta = \frac{J}{m} \frac{m^3}{kg} = \frac{J}{kg}$   
 $h_1 = 1742.1$   
 $h_2 = 1336.68$   
 $h_3 = 173.88$   
 $\frac{\dot{W}_p}{\dot{m}} = \eta_3 (h_u - P_3) = 1.00001 \cdot 10^{-3} (90 \cdot 10^5 - 100 \cdot 10^5)$   
 $= 9.067 \text{ kJ/kg} = h_u - h_3$   
 $h_u = 182.717$   
 $\eta = 0.17$

### Stoomturbine

3) Temp out  
 $S_1 = 517432$   
 $P_1 = 20 \text{ bar}$   
 $h_1 = 2708 \text{ kJ/kg}$   
 $T_1 = 293 \text{ K}$   
 $w_{in} = 420 \text{ kJ/kg}$   
 $T_2 = T_1$

4) Calculate Quality @ 2  
 $w_e = h_1 - h_2 = 420 \text{ kJ/kg}$   
 $h_2 = h_1 - 420 = 2288 \text{ kJ/kg}$   
 $h_2 = h_f + x_2(h_g - h_f) = 2288 - 191.83$   
 $x_2 = \frac{h_2 - h_f}{h_g - h_f} = \frac{2288 - 191.83}{2586.7 - 191.83} = 0.877$

### Calculate isentropic efficiency

5) Calculate isentropic efficiency  
 $\eta_t = \frac{h_1 - h_2}{h_1 - h_{2s}}$   
 als isochoor:  $S_1 = S_{2s} = 517432$   
 $x_{2s} = \frac{S_{2s} - S_f}{S_g - S_f} = \frac{517432 - 0.693}{81701 - 0.693} = 0.627$   
 $h_{2s} = h_f + x_{2s}(h_g - h_f) = 0.627(2586.7 - 191.83) + 191.83$   
 $h_{2s} = 1812.34 \text{ kJ/kg}$   
 $\eta_t = \frac{h_1 - h_2}{h_1 - h_{2s}} = \frac{2708 - 2288}{2708 - 1812.34} = 0.904$

### Verdampen vloeistoffen

in vloeistof A bevinden zich B & C  
 Tijdens verdampen is op het moment  
 stoffen v B uit de vloeistof verdwenen  
 $\Rightarrow$  hoeveel C is er nog?

- dampspanning A is heel klein  $P_{A,0}$
  - verdampingsdruk vloeistof B =  $2 \cdot P_c$
  - activiteitscoëfficiënt v C in vloeistof 4x zo groot als die van B
- Raakt(1) law:

$$P_i = y_i P = P_{sat,i} \cdot x_i \cdot \gamma_i$$

- $P_A \approx 0$
- $P_{sat,B} = 2 \cdot P_{sat,C}$
- $\gamma_C = 4 \gamma_B$

moment 1: 50% v alk B uit vloeistof A verdwenen

als er een verdampingsflaks platform, geldt:

$$\frac{dn_i}{dt} = -k \cdot (A_{sat}) \cdot P_i \rightarrow \text{Dampspanning}$$

strome van het aantal mol van 'i' met de tijd

$x_i = \frac{n_i}{\sum n_i}$   
 opgem is dat A & B by concentraties hebben naar onder  
 En zijn niet veranderd ster  
 ic het in de constante k

$$= -k \cdot P_{sat,i} \cdot \gamma_i \cdot x_i$$

$$= -k \cdot P_{sat,i} \cdot \gamma_i \cdot \frac{n_i}{\sum n_i}$$

$$\frac{dn_i}{dt} = -k \cdot P_{sat,i} \cdot \gamma_i \cdot n_i$$

Differentiaal vgl oplossen door scheiden van variabelen

$$n_i(t) = n_i(0) \cdot \exp(-k \cdot t \cdot P_{sat,i} \cdot \gamma_i) = e^{-k \cdot t \cdot P_{sat,i} \cdot \gamma_i}$$

op een moment is er nog 10% v B  
 $n_B(t) = 1/6$

$$1/6 = \exp(-k \cdot t \cdot P_{sat,B} \cdot \gamma_B)$$

$$\ln(1/6) = -k \cdot t \cdot P_{sat,B} \cdot \gamma_B \Rightarrow k \cdot t = \frac{\ln(6)}{P_{sat,B} \cdot \gamma_B}$$

dit invullen in vgl voor C

$$\frac{n_C(t)}{n_C(0)} = e^{-(k \cdot t \cdot P_{sat,C} \cdot \gamma_C)}$$

$$= \exp\left(\frac{-\ln(6)}{P_{sat,B} \cdot \gamma_B} \cdot P_{sat,C} \cdot \gamma_C\right)$$

$$= \exp\left(\frac{-\ln(6) \cdot 4}{2}\right) = 1/4$$

$P_{A,0} \approx 0$   
 $P_{sat,B} = 2 \cdot P_{sat,C}$   
 $\gamma_C = 4 \gamma_B$

### Tasland vloeistof Gas

$P = c / (V \cdot T)$   
 $c = \text{constante}$   
 $V = \text{molecul volume}$   
 $T = \text{temperatuur}$   
 $b = 5 \cdot 10^{-5} \text{ mol}$   
 $C = 40 \frac{\text{mol}}{\text{m}^3}$   
 $\Rightarrow \text{moleculair gewicht van T}$

1) Moleculair gewicht:  $C = \frac{m}{V} = \frac{C}{M} \Rightarrow M = \frac{C}{C}$   
 in de liter van by de druk geëngst elk mol vloeistof  
 2) last van dat Cp niet afhangt van druk  
 $\left(\frac{\partial C_p}{\partial P}\right)_T = 0 \Rightarrow \text{and } C_p = \text{const}$

3) bereken enthalpie afname  
 $h(T_2) - h(T_1) = \int_{T_1}^{T_2} C_p dT$   
 $v = \frac{m}{\rho} = \frac{m}{C} = \frac{1}{C}$   
 $\frac{\partial h}{\partial T} = C_p$   
 $v \cdot T \left(\frac{\partial h}{\partial T}\right) = \int_{T_1}^{T_2} v \cdot C_p dT = \frac{v}{C} \cdot C_p \cdot (T_2 - T_1)$   
 enthalpie afname =  $\int_{T_1}^{T_2} v \cdot C_p dT = \frac{1}{C} \cdot C_p \cdot (T_2 - T_1) = 500 \text{ J/kg}$

### Evenwichts reactie ideaal gas

1) bereken K  
 $A + B \leftrightarrow C + D$   
 evenwicht: 1 mol A, 1 mol B, 2 mol C, 1 mol D  
 $P_i = P \cdot y_i$   
 $y_i = \frac{n_i}{\sum n_i}$   
 $P_i = \frac{n_i P}{V}$   
 $K = \frac{P_C \cdot P_D}{P_A \cdot P_B} = \frac{n_C \cdot n_D}{n_A \cdot n_B} \left(\frac{P}{V}\right)^{\Delta n}$   
 $= \frac{2}{1} = 2$

### 1) Mol A toegevoegd bereken $y_A$ na evenwicht

$n_A = 2 - x$   
 $n_B = 1 - x$   
 $n_C = 2 + x$   
 $n_D = 1 + x$   
 $n = 6$   
 $K = \frac{y_C \cdot y_D}{y_A \cdot y_B} = 2$   
 $\frac{2+x}{6} \cdot \frac{1+x}{6} = 2 \cdot \frac{2-x}{6} \cdot \frac{1-x}{6}$   
 $(2+x)(1+x) = 2(2-x)(1-x)$   
 $2 + 3x + x^2 = 2(2 - 3x + x^2)$   
 $x^2 - 3x + 2 = 0$   
 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{3 \pm \sqrt{9 - 4}}{2} = 1.5$   
 $x = 1.5$   
 $n_A = 2 - 1.5 = 0.5$   
 $y_A = \frac{0.5}{6} = 0.083 \text{ mol\%}$

### Productie proces met een Compressor

3) bereken opbrengst van B  
 opbrengst B =  $\frac{\text{mol A geproduceerd}}{\text{mol A per uur}} = 0.6$   
 $\eta_B = \frac{0.6 \cdot 100}{100} = 0.6$

4, 5)

	1	2	3	4	5	6	7
A	100	$y = 156.25$	$0.04 y = 62.5$	0	0.04 y = 187.5	0	$0.04 y \cdot f = 0.04 y \cdot (-1)$
B	0	0	0	0	0	0	0
I	1	$x = 10$	0	0	x	$x \cdot f = 1$	$x \cdot (-f)$
Tot	101	$y + 10$	0	0	0	0	0

$1 = x \cdot f$   
 $f = 0.1$   
 $x = 10$   
 $I \cdot f = 10 \text{ mol\%}$   
 $y = 100 + 0.04 y \cdot (-1)$   
 $y = 156.25 = 156.25 \text{ mol\%}$

6)  $\eta_B = \frac{93.25}{100} = 0.9325$

### Batch reactor

#### 1) Bereken omzetting van 2<sup>o</sup> orde reactie $2A \rightarrow B$

$\frac{dC_A}{dt} = -k C_A^2$   
 $\int_{C_{A0}}^{C_A} \frac{1}{C_A^2} dC_A = -k \int_0^t dt$   
 $-\frac{1}{C_A} = -kt$   
 $\frac{1}{C_A} = kt + \frac{1}{C_{A0}}$   
 $\frac{C_{A0}}{C_A} = C_{A0} kt + 1$   
 $\frac{1}{C_{A0} kt + 1} = \frac{C_A}{C_{A0}}$   
 $S_0 = 1 - \frac{C_A}{C_{A0}} = \frac{C_{A0} kt}{1 + C_{A0} kt}$

8) hoeveel water na 600s geleverd?  $\Delta h = -50 \text{ kJ mol}^{-1}$

$Q = (\text{tot aantal mol omgezet}) \cdot (\Delta h \cdot \text{mol}^{-1})$   
 $= -\sum n_i \cdot C_{A0} \cdot V \cdot (-\Delta h / 2)$

Vloeistof mengsel 50 mol% water & 50 mol% ethanol kookt by 1.1 bar  $\Rightarrow$  grafiek

$\Rightarrow$  Raoult gebruiken:

$w = \text{water}$   $e = \text{ethanol}$

$P = 1.1 \text{ bar}$

$P_i = \gamma_i P = P_{sat,i} \cdot x_i \cdot \gamma_i$   
 $\gamma_i = 1$  (ideaal v.)

$P = 1.1 = P_{sat,w} \cdot x_w + P_{sat,e} \cdot x_e$  ( $x_w + x_e = 1$ )  
 $= P_{sat,w} \cdot x_w + P_{sat,e} \cdot (1 - x_w)$

$\Rightarrow$  50-50 mengsel, dus  $x_w = 1/2 = x_e$

$\Rightarrow 1.1 = P_{sat,w} \cdot 1/2 + P_{sat,e} \cdot 1/2$

$P_{sat,w} + P_{sat,e} = 2.2 \text{ bar}$

in de grafiek nu zoeken naar een verticale lijn, opgeteld zit het.

